## MATH 1300 ASSIGNMENT PROBLEMS (UNIT 5)

[10] 1. Use a third row cofactor expansion to evaluate the determinant of

$$\mathbf{A} = \begin{bmatrix} 5 & 1 & 4 & 1 \\ 4 & 1 & 2 & 5 \\ 2 & 3 & 4 & 1 \\ 1 & 1 & 2 & 4 \end{bmatrix}.$$

[10] 2. Compute the determinant of  $A = \begin{bmatrix} 8 & 6 & 6 & 5 \\ 2 & 4 & 6 & 2 \\ 6 & 9 & 7 & 5 \\ 5 & 6 & 3 & 1 \end{bmatrix}$  by the method of using elementary

row operations to transform the matrix A into an upper triangular matrix.

[10] 3. Let 
$$A = \begin{bmatrix} 1 & 3 & 4 \\ 2 & 4 & 1 \\ 1 & 2 & 3 \end{bmatrix}$$
.

- (a) Find the matrix adj(A).
- (b) Compute the matrix product  $A \cdot adj(A)$ .
- (c) Use the information from part (b) to determine the value of det(A). Explain.
- (d) Use the information from parts (a) and (c) to find the inverse matrix  $A^{-1}$ .
- [10] 4. Use Cramer's rule to solve the following system of linear equations.

$$x+3y+z=2$$
$$3x+2y+z=2$$
$$4x+y+3z=3$$

- [10] 5. Let A and B be  $3 \times 3$  matrices with det(A) = 2 and det (B) = 6. Determine the values of the following.
  - (a) det(AB)
  - (b)  $det(A^{-1}B)$
  - (c)  $det(A^{T}B^{-1})$
  - (d) det(5A)
  - (e) det(adj(AB))

[10] 6(a) Let  $A = \begin{bmatrix} k & -3 \\ 1 & k-4 \end{bmatrix}$ . For what values of k is the matrix A noninvertible?

(b) Let  $B = \begin{bmatrix} 1 & 1 & 1 \\ 2 & k & 1 \\ 3 & 1 & k \end{bmatrix}$ . For what values of k is the matrix B noninvertible?