MATH 1300 ASSIGNMENT PROBLEMS (UNIT 5)

[10] 1. Use a third row cofactor expansion to evaluate the determinant of

$$A = \begin{bmatrix} 5 & 1 & 4 & 1 \\ 4 & 1 & 2 & 5 \\ 2 & 3 & 4 & 1 \\ 1 & 1 & 2 & 4 \end{bmatrix}.$$

[10] 2. Compute the determinant of $A = \begin{bmatrix} 8 & 6 & 6 & 5 \\ 2 & 4 & 6 & 2 \\ 6 & 9 & 7 & 5 \\ 5 & 6 & 3 & 1 \end{bmatrix}$ by the method of using elementary

row operations to transform the matrix A into an upper triangular matrix.

[10] 3. Let
$$A = \begin{bmatrix} 1 & 2 & 0 \\ 3 & 2 & 1 \\ 1 & 2 & 3 \end{bmatrix}$$
.

- (a) Find the matrix adj(A).
- (b) Compute the matrix product $A \cdot adj(A)$.
- (c) Use the information from part (b) to determine the value of det(A). Explain.
- (d) Use the information from parts (a) and (c) to find the inverse matrix A^{-1} .
- [10] 4. Use Cramer's rule to solve the following system of linear equations.

$$x + 3y + z = 2$$

$$3x + 2y + z = 2$$

$$4x + y + 3z = 3$$

- [10] 5. Let A and B be 3×3 matrices with det(A) = 2 and det(B) = 6. Determine the values of the following.
 - (a) det(AB)
 - (b) $det(A^{-1}B)$
 - (c) $det(A^TB^{-1})$
 - (d) det(5A)
 - (e) det(adj(AB))
- [10] 6(a) Let $A = \begin{bmatrix} k+1 & 4 \\ 1 & k-2 \end{bmatrix}$. For what values of k is the matrix A noninvertible?
 - (b) Let $B = \begin{bmatrix} 1 & 1 & 1 \\ 2 & k & 6 \\ 3 & 2 & 1 \end{bmatrix}$. For what values of k is the matrix B noninvertible?