

MATH 1300 ASSIGNMENT PROBLEMS (UNIT 3)

- [4] 1. (a) There are 4 possible row-reduced echelon forms of a 2×2 matrix. What are they?
- [6] (b) Give an example of two distinct 2×2 nonzero matrices A and B such that $AB = 0$
- [10] 2. Use Gaussian elimination procedure: back substitution to solve the following systems of equations.

$$\begin{array}{ll} x + y - z = 0 & 2x - y + z = 0 \\ \text{a) } 2x - y + z = 6 & \text{b) } x - 2y + 3z = 3 \\ 3x - y + 2z = 11 & 4x - 5y + 7z = 6 \end{array}$$

- [10] 3. Use Gauss Jordan elimination procedure to solve the following systems. You must reduce the matrix to its row reduced echelon form and then write the complete solution to the system.

$$\begin{array}{ll} x - 2y + z = 3 & w + 2x - y + z = 6 \\ \text{a) } 2x + y - z = -8 & \text{b) } 2w - x + 2y - z = 3 \\ 3x + 2y + 3z = 1 & 4w + 3x + z = 15 \\ & w - 2x + 3y - 2z = 8 \end{array}$$

- [10] 4. The augmented matrix from a system of linear equations has the following reduced row-echelon form.

$$\left[\begin{array}{ccccccc|c} 1 & 2 & 0 & 1 & 0 & 3 & 0 & 1 \\ 0 & 0 & 1 & 4 & 0 & 5 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 1 & 0 & 2 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 3 \end{array} \right]$$

- (a) How many equations are there in the system?
- (b) How many variables are there in the system?
- (c) How many parameters are there in the solution set?
- (d) Write out the solution set for the system

[10] 5. Consider the system of linear equations

$$x + 2y + z = 3$$

$$2x + 5y + 3z = 7 \quad \text{where } k \text{ is a real number.}$$

$$3x + 7y + 4z = k$$

- (a) Write out the augmented matrix for this system of linear equations.
- (b) Use elementary row operations to reduce the augmented matrix to row-echelon form.
- (c) For what values of k does the system have solutions? Find all such solutions.
- (d) For what value of k does the system have no solution?

[10] 6. Jill, Shirley and Kate went to their local produce store to buy some fruit. Jill bought three pounds of bananas and two pounds of grapes and paid \$5.70. Shirley bought two pounds of bananas and two pounds of nectarines and paid \$6.20. Kate bought three pounds of grapes and a pound of nectarines and paid \$7.80.

- (a) Let x = price of a pound of bananas, y = price of a pound of grapes and z = price of a pound of nectarines. Write out 3 linear equations representing the purchases Jill, Shirley and Kate.
- (b) Write out the augmented matrix for your system of 3 linear equations of part (a).
- (c) Use elementary row operations to row reduce the augmented matrix of part (b) to a reduced row-echelon matrix.
- (d) What is the price per pound for each of the three fruits?