[20] 1. Use the corner point method to solve the following linear programming problems.

(a) Find the maximum value of Z = 20x + 30y subject to the following constraints:  $-x + 2y \le 40$ ,  $x + 4y \ge 54$ ,  $3x + y \le 63$ ,  $x \ge 0$ ,  $y \ge 0$ 

(b) Find the minimum value of Z = 5x + 3y subject to the following constraints:  $3x + y \ge 30$ ,  $4x + 3y \ge 60$ ,  $x + 2y \ge 20$ ,  $x \ge 0$ ,  $y \ge 0$ 

- [10] 2. A trucker is asked to deliver 2 kinds of desks to a furniture store. The standard desk weighs 50 kilos and the deluxe desk weighs 75 kilos. The truck has a capacity of at most 30 desks. In addition, weight restrictions only allow for the truck to carry at most 1800 kilos. If the trucker receives \$15 for each standard desk and \$20 for each deluxe desk that he delivers, how many desks of each type should he carry in order to maximize his income?
- [15] 3. Use the simplex method to maximize p = 5x + 4y + 3z subject to the constraints:

 $x \ge 0$ ,  $y \ge 0$ ,  $z \ge 0$ ,  $x + y + z \le 30$ ,  $2x + y + 3z \le 60$ ,  $3x + 2y + 4z \le 84$ 

[15] 4. Use the simplex method to find the maximum value of p = 10x + 5y + 12z subject to the constraints.

 $x + 3y + 2z \le 60$ ,  $2x + y + 3z \le 60$ ,  $2x + y + 2z \le 42$ ,  $x \ge 0$ ,  $y \ge 0$ ,  $z \ge 0$ .