

# MATH 1500 Assignment 4

(Follows Unit 11 in the manual)

## Values

[12] 1. Find the critical numbers of each of the following functions. [cf. Section 4.1]

(a)  $f(x) = x^4 - 2x^2$       (b)  $f(x) = xe^{2x}$       (c)  $f(x) = 3x^{1/3} - x$

[12] 2. Find the absolute maximum and absolute minimum values of  $f(x)$  on the given interval. [cf. Section 4.1]

(a)  $f(x) = 6x^2 - x^3$      $[-3, 5]$       (b)  $f(x) = 3x^{1/3} - x$      $[-2, 2]$

[8] 3. Verify that the function  $f(x) = x^3 + 3x$  satisfies the hypotheses of the Mean Value Theorem on the interval  $[0, 2]$ . Find all numbers  $c$  that satisfy the conclusion of the Mean Value Theorem. [cf. Section 4.2]

[12] 4. Determine the interval(s) where  $f(x)$  is increasing or decreasing. Find also the local maximum and local minimum values of  $f(x)$ .

(a)  $f(x) = \frac{x}{(1+x)^2}$       (b)  $f(x) = x^3 - 3x^2 + 5$

[10] 5. Determine where  $f(x) = x^4 - 4x^3$  is concave up and where it is concave down. Find all the inflection points of  $f(x) = x^4 - 4x^3$ . [cf. Section 4.3]

[16] 6. If  $f(x) = \frac{x^2 - 1}{x^2 - 4}$ , then  $f'(x) = \frac{-6x}{(x^2 - 4)^2}$  and  $f''(x) = 6 \left[ \frac{3x^2 + 4}{(x^2 - 4)^3} \right]$ .

(a) Determine the intervals where  $f(x)$  is increasing and where it is decreasing.

(b) Find all local maxima and all local minima.

(c) Determine where  $f(x)$  is concave up and where it is concave down.

(d) Find all inflection points.

(e) Find all horizontal asymptotes and all vertical asymptotes.

(f) Sketch the graph of  $f(x)$ . [cf. Section 4.5]

**Total = 70**