

MATH 1700 **ASSIGNMENT 3**

1. Compute

a. $\int \frac{1}{x^3+x^5} dx$ on an interval which does not contain $x = 0$

b. $\int \frac{x+1}{x^4+x^2+1} dx$

c*. $\int \frac{x^4+1}{x^3+1} dx$

2. Compute the following limits:

a. $\lim_{x \rightarrow \infty} x^n e^{-x}$ ($n \in \mathbb{N}$, $n \geq 1$).

b. $\lim_{x \rightarrow \infty} \frac{7x^3 + x^2}{2x^3 - 100}$

c. $\lim_{x \rightarrow \infty} \frac{1}{\sqrt{x^2 + 1}}$

d. $\lim_{x \rightarrow 0^+} \frac{x e^{-\frac{1}{x}}}{\tan^2 x}$

e. $\lim_{x \rightarrow \infty} \left(x - x^2 \ln \frac{1+x}{x} \right)$

3. Find

a. $\int_0^{\frac{\sqrt{3}}{2}} \sqrt{1-x^2} dx$

b. $\int \frac{x^3}{\sqrt{9-x^2}} dx$

c**. $\int_{\frac{\pi}{3}}^{\frac{\pi}{2}} \frac{1}{\sin x} dx$