

UNIVERSITY OF MANITOBA

MATH 1700 D01

Assignment 2

This assignment is based on units 3 and 4. **SHOW ALL WORK** to get full marks. Leave answers as exact answers. For example, leave it as $1/7$ as opposed to 0.142857.

1.

Sketch the region bounded between the curves $y = \sin x$, $y = \sin 2x$, $x = 0$, $x = \pi$. Find the area of this region.

2.

Let R be the region in the first quadrant bounded by the graphs of $x = y^3$ and $x = 4y$. Which is greater, the volume of the solid generated when R is revolved about the x -axis or the y -axis?

3.

Sketch the region R bounded by the curves $y = 1/\sqrt{x}$, $x = 1$, $x = 4$, and $y = 0$. Set up, but **DO NOT EVALUATE**, integrals that can be used to find the volume of the solid generated if R is revolved about the x -axis

(a) using cylindrical shells,

(b) using disks or washers.

4.

Evaluate.

(a) $\int_0^1 \frac{x^3}{\sqrt{x^2 + 1}} dx$ (hint: use integration by part)

(b) $\int e^{4x} \sin 5x dx$ (hint: use integration by part)

(c) $\int \frac{\cos^3 x}{\sqrt{\sin x}} dx$

(d) $\int \sin^4 x \cos^2 x dx$.