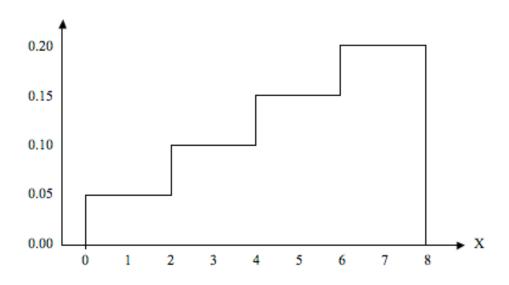
Sample Term Test 2A

1. A variable X has a distribution which is described by the density curve shown below:



What proportion of values of X fall between 1 and 6?

- (A) 0.550
- (B) 0.575
- (C) 0.600
- (D) 0.625
- (E) 0.650

2. Which of the following statements about a normal distribution is true?

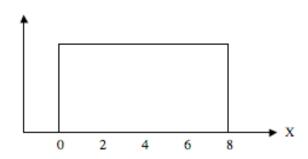
- (A) The value of μ must always be positive.
- (B) The value of σ must always be positive.
- (C) The shape of a normal distribution depends on the value of μ .
- (D) The possible values of a standard normal variable range from -3.49 to 3.49.
- (E) The area under a normal curve depends on the value of σ .

3. A variable X has a uniform distribution on the interval from 2 to 6.

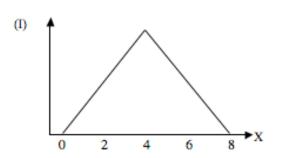
The P(4.2 < X < 5.7) is equal to:

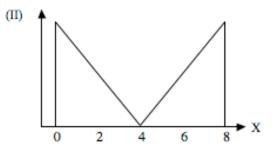
- (A) 0.375
- (B) 0.475
- (C) 0.575
- (D) 0.675
- (E) 0.775

4. A variable X follows a uniform distribution, as shown below:



The distribution of X has an interquartile range equal to 4 (since the middle 50% of the data are contained between the values 2 and 6). Consider the variables with the distributions shown below (assume that the heights of the curves are such that they are both valid density curves):





The interquartile range of density curve (I) is _____ and the interquartile range of density curve (II) is _____.

- (A) (I) less than 4, (II) greater than 4
- (B) (I) greater than 4, (II) less than 4
- (C) (I) equal to 4, (II) equal to 4
- (D) (I) less than 4, (II) less than 4
- (E) (I) greater than 4, (II) greater than 4

5.	A variable Z has a standard normal distribution. What is the value b such that $P(-0.37 \le Z \le b) = 0.5749$?				
	(A) 2.02	(B) 1.48	(C) 0.97	(D) 0.63	(E) 1.72
6.	What is the $P(Z$	> -0.75)?			
	(A) 0.2266	(B) 0.7734	(C) 0.0401	(D) 0.9599	(E) 0.4289
The	e next three quest	ions (7 to 9) refer	to the following:		
	The sport of wor scores for each eve deviations:				
		Event	Mean S	td. Dev.	
		Balance	Beam 8.3	0.3	
		Uneven l	Bars 8.6	0.5	
		Vault	8.2	0.4	
		Floor Ex	ercise 9.0	0.2	
7.	What proportion (A) 0.2088	of gymnasts receiving (B) 0.3674	ves a score betwee (C) 0.6000	en 8.2 and 8.7 on (D) 0.6837	the uneven bars? (E) 0.3085
8.	The top 6% of gyr is the minimum v		_		pionships. What
	(A) 8.44	(B) 7.58	(C) 8.90	(D) 8.41	(E) 8.82
9.	Julie receives a sevault and a 9.3 or gymnasts?				
	(A) Balance Bear	n			
	(B) Uneven Bars				
	(D) Oneven Dars				

(C) Vault

(D) Floor Exercise

(E) Julie did equally well on all events.

10.	Suppose that the variable Z follows a standard normal distribution. If $P(-b < Z < b) = 0.92$, then b is approximately:				
	(A) 1.75	(B) 1.41	(C) 0.82	(D) 1.64	(E) 0.96
11.	A variable X has the values of X fadeviation σ ?				
	(A) 5	(B) 7.5	(C) 12.5	(D) 15	(E) 30
12.	Speeds of vehicles standard deviation above the 100 km	n 8.7 km/h. What			•
	(A) 0.7126	(B) 0.2612	(C) 0.7910	(D) 0.2874	(E) 0.7611
13.	The time to comp mean of 90 minute will take longer th	es and a standard of	deviation of 10 min	nutes. What perce	
	(A) 50.00%	(B) 69.15%	(C) 30.85%	(D) 19.15%	(E) 22.85%
14.	The time it takes 58.47 seconds and race in exactly 60	standard deviation			
	(A) 0.0556	(B) 0.1736	(C) 0.0122	(D) 0.0409	(E) 0.0000
15.	Percentage grades and standard dev distribution with in Calculus. Wha	iation 10. Percenmean 68 and star	tage grades in a landard deviation 8.	arge English class Katherine receiv	follow a normal red a grade of 85
	(A) 87	(B) 88	(C) 89	(D) 90	(E) 91

16.	Bottles of a certain brand of apple juice are filled automatically by a machine.	Fill
	volumes are normally distributed with a mean of μ and standard deviation of 1.46	ml.
	The label on the bottles claim that the bottles contain 500 ml of juice. What ve	alue
	should μ be set at so that only 2% of bottles will be underfilled?	

- (A) 497 ml (B) 498 ml (C) 502 ml (D) 503 ml (E) 504 ml
- 17. A normal quantile plot is a useful tool to determine whether it is plausible that a variable has a normal distribution. Using a normal quantile plot, we conclude that a normal distribution is a reasonable assumption if:
 - (A) all points fall close to a straight horizontal line.
 - (B) all points fall close to a straight vertical line.
 - (C) all points fall close to a straight diagonal line.
 - (D) all points fall close to a bell-shaped curve.
 - (E) the points appear randomly scattered.
- 18. It is known that 53% of students at a large university are female and 47% are male. If we take a random sample of 12 students at the university, what is the probability that exactly seven of them are female?
 - (A) 0.1734 (B) 0.1834 (C) 0.1934 (D) 0.2034 (E) 0.2134
- 19. From past records, the professor of a large university course has established the following distribution for grades received by students in the course (with some values missing):

What is the probability of getting a grade of C+ or better?

- (A) 0.50
- (B) 0.62
- (C) 0.76
- (D) impossible to calculate without at least one of the missing probabilities.
- (E) impossible to calculate without both of the missing probabilities.

20. The number of courses X taken in one term by students at a large university has the probability distribution shown below, where k is some constant:

What is the probability that a randomly selected student is taking at least 3 courses in one term?

(A) 0.81

(B) 0.53

(C) 0.76

(D) 0.88

(E) 0.69

The next two questions (21 and 22) refer to the following:

The following five games are scheduled to be played at the World Curling Championship one morning. The values in parentheses are the probabilities of each team winning their respective game.

Game 1: Finland (0.43) vs. Germany (0.57) Game 2: USA (0.28) vs. Switzerland (0.72) Game 3: Japan (0.11) vs. Canada (0.89) Game 4: Denmark (0.33) vs. Sweden (0.67)

Game 5: France (0.18) vs. Scotland (0.82)

21. The outcome of interest is the set of winners of the five games. How many outcomes are contained in the sample space?

(A) 5

(B) 10

(C) 25

(D) 32

(E) 64

22. In a sports game, the "favourite" is the team with the higher probability of winning and the "underdog" is the team who is less likely to win. What is the probability that at least one underdog wins?

(A) 0.93

(B) 0.74

(C) 0.80

(D) 0.67

(E) 0.59

23. A manufacturer of automobile batteries claims that the distribution of battery lifetimes has a mean of 54 months and a variance of 36 months squared. Suppose a consumer group decides to check the claim by purchasing a sample of 50 of these batteries and subjecting them to tests to determine their lifetime. Assuming the manufacturer's claim is true, what is the probability that the sample has a mean lifetime less than 52 months?

(A) 0.1292

(B) 0.3707

(C) 0.0091

(D) 0.4909

(E) 0.3483

24. A recently married couple plans to have two children. The outcome of interest is the gender of each of the two children. Consider the event that exactly one of the couple's children will be a boy. Which of the following is the complement of this event?	
(A) two boys	
(B) two girls	
(C) one girl	
(D) at least one girl	
(E) zero or two girls	
25. A recycling plant compresses aluminum cans into bales. The weights of the bales are known to follow a normal distribution with standard deviation eight pounds. In a random sample of 64 bales, what is the probability that the sample mean differs from the population mean by no more than one pound?	
(A) 0.3413 (B) 0.4772 (C) 0.6826 (D) 0.9544 (E) 0.1587	
26. The monthly mortgage payment for recent home buyers in Winnipeg has a mean of	

\$732, and a standard deviation of \$421. A random sample of 125 recent home buyers is selected. The approximate probability that their average monthly mortgage payment

(C) 0.4082

27. Weights of pears in an orchard follow a normal distribution with mean 195 grams and standard deviation 40 grams. A random sample of five pears is selected. What is the probability that the total weight of the pears is greater than one kilogram (i.e., 1,000

(C) 0.2451

(D) 0.0478

(D) 0.3264

(E) 0.0918

(E) 0.4129

will be more than \$782 is:

(A) 0.9082

grams)?

(A) 0.2795

(B) 0.4522

(B) 0.3897

- 28. The fact that the sample mean does not tend to over- or underestimate the population mean makes the sample mean:

 (A) resistant.
 (B) unbiased.
 (C) efficient.
 (D) a statistic.
 (E) a parameter.

 29. A random variable X follows a uniform distribution with mean 3 and standard deviation 1.73. We take a random sample of size 100 from this distribution and calculate the sample mean X̄. The sampling distribution of X̄ is:
 - (A) approximately normal with mean 3 and standard deviation 0.173.
 - (B) uniform with mean 3 and standard deviation 1.73.
 - (C) approximately normal with mean 3 and standard deviation 0.0173.
 - (D) uniform with mean 3 and standard deviation 0.173.
 - (E) approximately normal with mean 3 and standard deviation 1.73.
 - 30. The sampling distribution of a statistic is:
 - (A) the density function of the population from which the sample was selected.
 - (B) the distribution of values taken by the statistic in all possible samples of the same size from the same population.
 - (C) the distribution of the population from which the sample is drawn.
 - (D) approximately normally distributed if the sample is large enough, regardless of the shape of the population from which the sample is drawn.
 - (E) all of the above.
 - 31. There are four patients on the neo-natal ward of a local hospital who are monitored by two staff members. Suppose the probability (at any one time) of a patient requiring attention by a staff member is 0.3. Assuming the patients behave independently, what is the probability at any one time that there will not be sufficient staff to attend to all patients who need them?
 - (A) 0.0756 (B) 0.1104 (C) 0.0837 (D) 0.0463 (E) 0.2646

32. According to the Canadian Blood Services website, 9% of Canadians have type B blood. If a sample of 8 donors is selected, what is the probability that less than two of them will have type B blood?

(A) 0.8424

(B) 0.9711

(C) 0.3721

(D) 0.4703

(E) 0.1576

33. Which of the following variables has a binomial distribution?

- (I) You repeatedly roll a fair die.
 - X = number of rolls needed to observe the number 6 for the third time.
- (II) Tim Horton's is holding its annual "Roll Up the Rim to Win" promotion. Customers can check under the rim of a coffee cup to see if they have won a prize. You buy one cup of coffee from Tim Horton's each day for a week.

X = number of times you win a prize during the week.

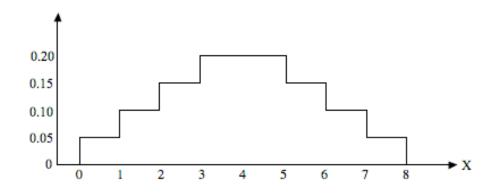
(III) A quality control inspector in a factory routinely examines samples of fiber-optic cable being produced to check for defects. The inspector examines a 100-foot length of cable.

X = number of defects found on the cable.

- (A) I only
- (B) II only
- (C) I and II only
- (D) II and III only
- (E) I, II, and III

Sample Term Test 2B

1. A random variable X is described by the density curve shown below:



The probability of $P(3 \le X \le 6)$ is equal to:

- (A) 0.55
- (B) 0.45
- (C) 0.375
- (D) 0.40
- (E) 0.60

2. A random variable X follows a uniform distribution on the interval from 10 to 15. What proportion of values of X are greater than 13.2?

- (A) 0.18
- (B) 0.88
- (C) 0.36
- (D) 0.12
- (E) 0.28

3. Which of the following statements about a normal distribution is true?

- (A) The mean of a normal distribution must always be greater than zero.
- (B) For a standard normal distribution, P(Z < z) = P(Z > -z) for any value z.
- (C) The height of a normal density curve must always be equal to one.
- (D) All values must fall within three standard deviations of the mean.
- (E) The standard deviation of a normal distribution must always be greater than one.

4.	10. The maximum maximum height	Y follows a norm im height of the for the density co	stribution with mal distribution with density curve for Y , and there a under the den	th mean 25 and story X is a near a under the	andard deviation (i) the
	(A) (i) greater th	an, (ii) less than			
	(B) (i) less than,	(ii) greater than			
	(C) (i) equal to,	(ii) equal to			
	(D) (i) greater th	an, (ii) equal to			
	(E) (i) less than,	(ii) less than			
5.	_	It is known that	hard are known to approximately 99. andard deviation o	7% of apples have	weights between
	(A) 9 grams	(B) 12 grams	(C) 18 grams	(D) 24 grams	(E) 36 grams
6.	A variable Z has $P(b \le Z \le 0.36)$		al distribution. W	hat is the value b	such that
	(A) -1.22	(B) -0.68	(C) -0.27	(D) -0.39	(E) -0.55
Γ h ϵ	e next two questic Percentage grades and standard dev	s in a large geogra	to the following: phy class follow a	normal distributio	n with mean 67.5
7.	What proportion	of students in the	e class receive per	centage grades bet	tween 60 and 70?
	(A) 0.2650	(B) 0.2750	(C) 0.2850	(D) 0.2950	(E) 0.3050
8.	The professor dec grades, and a gra student needs to	ade of A to the r	next best 12%. W		_
	(A) 77	(B) 78	(C) 79	(D) 80	(E) 81

9.	The contents of bottles of water follow a normal distribution with mean μ and standard deviation 4 ml. What proportion of bottles have fill volumes within 1 ml of the mean?
	(A) 0.1974
	(B) 0.5987
	(C) 0.6826
	(D) 0.4013
	(E) unable to calculate without the value of μ
10.	A candy company manufactures hard candies in five different flavours, according to the following probability distribution, where k is some constant:
	Flavour Cherry Root Beer Strawberry Orange Peppermint
	Probability 0.21 k 0.27 k 0.14
	If you select a candy at random, what is the probability that it will be fruit-flavoured?
	(A) 0.48 (B) 0.67 (C) 0.68 (D) 0.72 (E) 0.86
11.	Event A has probability of 0.4 to occur and Event B has a probability of 0.5 to occur. Their union (A or B) has a probability of 0.7 to occur. Then:
	(A) A and B are mutually exclusive.
	(B) A and B are not mutually exclusive.
	(C) A and B are independent.
	(D) A and B are dependent.
	(E) both (B) and (C).
12.	You have two unfair coins. On any given flip, the first coin has a 40% chance of landing on Heads and the second coin has a 25% chance of landing on Heads. If you flip both

coins, what is the probability that at least one of them lands on Heads?

(B) 0.45

(C) 0.55

(D) 0.65

(E) 0.90

(A) 0.10

13. Suppose it is known that 8% of males are colour blind. In a random sample of 20 males, what is the probability that exactly 3 of them are colour blind?			sample of 20 males,		
(A) 0.1212	(B) 0.1313	(C) 0.1414	(D) 0.1515	(E) 0.1616	
and define l	led die will be rolled. B to be the event the intersection of A an	nat a prime numb			
(A) $\{2\}$					
(B) $\{2, 3, 5\}$					
(C) $\{2, 3, 4,$	$5, 6$ }				
(D) $\{3,5\}$					
(E) $\{1, 2, 3,$	$4, 5, 6$ }				
read the Wi randomly se	15. Suppose it is known that 61% of Winnipeg adults read the Winnipeg Free Press, 29% read the Winnipeg Sun and 18% read both newspapers. What is the probability that a randomly selected adult in Winnipeg reads only one of the two papers (but not both)? Hint: Draw a Venn diagram.				
(A) 0.54	(B) 0.50	(C) 0.45	(D) 0.72	(E) 0.47	

1 ne	ne next two questions (16 and 17) refer to the following:				
	A hockey players compiles the following facts:				
	\bullet Her team wins (W) 60% of their games.				
	• She scores a goal (G) in 30% of her games.				
	• She gets a penalty (P) in 40% of her games.				
	• In 38% of	her games, her t	eam wins and she	scores a goal.	
	• In 24% of	her games, her t	eam wins and she	gets a penalty.	
	• in 15% of	her games, she se	cores a goal and g	ets a penalty.	
16.	In any given gar	me, what is the p	robability that the	e player scores a go	oal or gets a penalty?
	(A) 0.85	(B) 0.55	(C) 0.70	(D) 0.65	(E) 0.58
17.	Which of the fo	ollowing statemen	nts is true ?		
	(A) W and G are independent.				
	(B) G and P a	re mutually exclu	usive (disjoint).		
	(C) W and P are independent.				
	(D) W and G are mutually exclusive (disjoint).				
	(E) G and P as	re independent.			
18.	0	0	•		tion with mean 0.22 t four oranges, what

(C) 0.9332

(D) 0.7967

(E) 0.8340

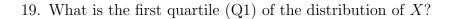
is the probability that their total weight is less than 1 pound?

(B) 0.8508

(A) 0.9719

The next two questions (19 and 20) refer to the following:

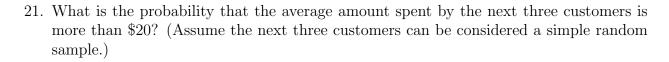
The time X taken by a cashier in a grocery store express lane follows a normal distribution with mean 90 seconds and standard deviation 20 seconds.



- (A) 73.8 seconds
- (B) 85.0 seconds
- (C) 69.4 seconds
- (D) 81.2 seconds
- (E) 76.6 seconds
- 20. What is the probability that the average service time for the next three customers is between 80 and 100 seconds? (Assume the next three customers can be considered a simple random sample.)
 - (A) 0.6156
 - (B) 0.4893
 - (C) 0.7212
 - (D) 0.5559
 - (E) impossible to calculate with the information given

The next two questions (21 and 22) refer to the following:

The amount X spent (in \$) by customers in the grocery store express lane follow some right-skewed distribution with mean \$24 and standard deviation \$15.



- (A) 0.4619
- (B) 0.6772
- (C) 0.8186
- (D) 0.7673
- (E) impossible to calculate with the information given

22. What is the probability that the next 40 customers spend less than \$1,000 in total? (Assume the next 40 customers can be considered a simple random sample).

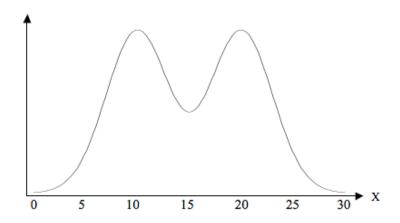
- (A) 0.5199
- (B) 0.6064
- (C) 0.6628
- (D) 0.5784
- (E) 0.6331

23. The distribution of weights of chocolate bars produced by a certain machine is normal with mean 253 grams and standard deviation 3 grams. A sample of five of these chocolate bars is selected. There is only a 2.5% chance that the average weight of the sample will be below:

- (A) 250.37 grams.
- (B) 254.10 grams.
- (C) 252.63 grams.
- (D) 251.54 grams.
- (E) 249.82 grams.

The next two questions (24 and 25) refer to the following:

A bimodal probability distribution is one with two distinct peaks. A random variable X follows a bimodal distribution with mean 15 and standard deviation 4, as shown below:



- 24. Suppose that you take a random sample of 10,000 observations from the population above and make a histogram. You expect the histogram to be:
 - (A) approximately normal with mean close to 15 and standard deviation close to 0.0004.
 - (B) bimodal with mean close to 15 and standard deviation close to 0.04.
 - (C) approximately normal with mean close to 15 and standard deviation close to 0.04.
 - (D) bimodal with mean close to 15 and standard deviation close to 4.
 - (E) approximately normal with mean close to 15 and standard deviation close to 4.
- 25. Suppose that you take 10,000 random samples of 10,000 observations from the population above and that for each sample, the mean \bar{x} is calculated. A histogram of resulting \bar{x} 's would be:
 - (A) approximately normal with mean close to 15 and standard deviation close to 0.0004.
 - (B) bimodal with mean close to 15 and standard deviation close to 0.04.
 - (C) approximately normal with mean close to 15 and standard deviation close to 0.04.
 - (D) bimodal with mean close to 15 and standard deviation close to 4.
 - (E) approximately normal with mean close to 15 and standard deviation close to 4.

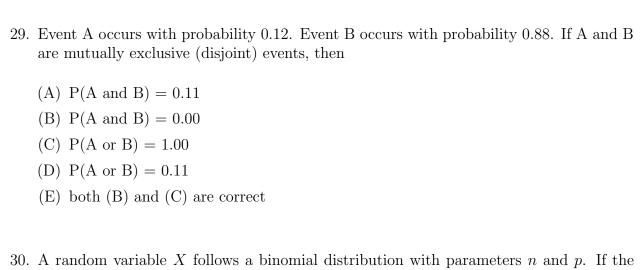
26. The Central Limit Theorem states that:

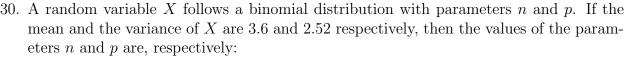
- (A) when n gets large, the standard deviation of the sample mean \bar{X} gets closer and closer to σ/\sqrt{n} .
- (B) regardless of the population distribution of a random variable X, when n gets large, the sampling distribution of \bar{X} is approximately normal.
- (C) if a random variable X follows a normal distribution, then when n gets large, the sampling distribution of \bar{X} is exactly normal.
- (D) when n gets large, the sample mean \bar{X} gets closer and closer to the population mean
- (E) when n gets large, the sample mean \bar{X} becomes an unbiased estimator of the population mean μ .

27. Which of the following variables has a binomial distribution?

- (A) You roll five fair dice, each with face values of 1 through 6. X = total number of dots facing up on the five dice.
- (B) An airplane carrying 100 passengers has two emergency exits, one at the front of the plane and one at the back. The airplane makes an emergency landing. X = number of people who leave the plane through the front exit.
- (C) A paper boy delivers the newspaper to every house on your block. X = number of houses that get their newspaper on time tomorrow morning.
- (D) You repeatedly flip two quarters simultaneously until both quarters land on Heads. X = number of flips required for both quarters to land on Heads.
- (E) A student randomly guesses the answer to each of the 40 multiple choice questions on this exam.
 - X = number of multiple choice questions the student gets correct.
- 28. The probability that a certain machine will produce a defective item is $\frac{1}{4}$. If a random sample of six items is taken from the output of this machine, what is the probability that there will be at least five defectives in the sample?

- (A) $\frac{1}{4096}$ (B) $\frac{3}{4096}$ (C) $\frac{4}{4096}$ (D) $\frac{18}{4096}$ (E) $\frac{19}{4096}$





- (A) 6 and 0.6.
- (B) 18 and 0.2.
- (C) 24 and 0.15.
- (D) 12 and 0.3.
- (E) 12 and 0.4.
- 31. A student driving to university must pass through seven sets of traffic lights. Suppose it is known that each set of traffic lights are red 35% of the time and that all lights function independently. What is the probability that the student will have to stop at two or more sets of lights on her to university?
 - (A) 0.6828 (B) 0.2985 (C) 0.4893 (D) 0.7662 (E) 0.5997

The next three questions (32 and 34) refer to the following:

We have a small deck of ten cards. Five of the cards are red, three are blue and two are green. We randomly select **four** cards from the deck **with replacement**. That is, after we select a card and record the colour, we put the card back in the deck and thoroughly shuffle them before we select another card.

- 32. Let X be the number of blue cards that are selected. The distribution of X is:
 - (A) binomial with parameters n = 4 and p = 0.1.
 - (B) binomial with parameters n = 10 and p = 0.3.
 - (C) binomial with parameters n = 10 and p = 0.4.
 - (D) binomial with parameters n = 4 and p = 0.3.
 - (E) normal with parameters $\mu = 1.2$ and $\sigma = 0.92$.
- 33. Let A be the event that the first selected card is the only red card in our four selections. Which of the following events is mutually exclusive (disjoint) from the event A?
 - (A) Second card selected is blue.
 - (B) No green cards are selected.
 - (C) Third selected card is the only green.
 - (D) Same number of red and blue cards are selected.
 - (E) Same number of blue and green cards are selected.
- 34. What is the probability that the first two selected cards are the same colour?
 - (A) 0.38
- (B) 0.25
- (C) 0.29
- (D) 0.33
- (E) 0.41

Sample Term Test 2 – Solutions

Question	Sample Test A	Sample Test B	
1	A	A	
2	В	С	
3	A	В	
4	A	D	
5	В	В	
6	В	С	
7	В	E	
8	E	В	
9	A	A	
10	A	В	
11	В	E	
12	E	C C A A	
13	C	C	
14	E	A	
15	В	A	
16	D	В	
17	C	C	
18	E	C	
19	В	E	
20	D	A	
21	D	E	
22	C	C	
23	Γ	A	
24	E	A D	
25	Γ	С	
26	E	В	
27	В	E	
28	В	E	
29	A	E	
30	В	D	
31	С	D	
32	A	D	
33	В	E	
34		A	