1.	Annual salaries of workers in a large union follow a normal distribution with standard
	deviation \$10,000. What sample size is required if we want to estimate the true mean
	salary to within \$2,000 with 93% confidence?

(A) 82

(B) 85

(C) 88

(D) 94

(E) 97

- 2. A horticulturist wishes to estimate the true mean growth of seedlings in a large timber plot last year. A random sample of 20 seedlings is selected and the one-year growth for each of them is measured. The sampled seedlings have a mean growth of 5.6 cm and a standard deviation of 1.5 cm. One-year seedling growth is known to follow a normal distribution with standard deviation 2.0 cm. We wish to conduct a hypothesis test at the 10% level of significance to determine whether the true mean one-year seedling growth differs from 6.0 cm. The critical region for the test is:
 - (A) |z| > 1.645
 - (B) t < -1.328
 - (C) z < -1.282
 - (D) |t| > 1.729
 - (E) |z| > 1.282

3.	A random variable X follows a normal distribution with standard deviation $\sigma = 8$. We
	take a random sample of 25 individuals from the population and we calculate a confidence
	interval for μ to be (36.7136, 43.2864). What is the confidence level of this interval?

(A) 90%

(B) 95%

(C) 96%

(D) 98%

(E) 99%

- 4. A test of H_0 : $\mu = 100$ vs. H_a : $\mu \neq 100$ is conducted for the mean μ of some population. We take a sample of ten individuals and calculate a sample mean of 104. A 98% confidence interval for μ is calculated to be (101, 107). Which of the following statements is true?
 - (A) We fail to reject H₀ at a 4% level of significance, since 100 is not contained in the 98% confidence interval.
 - (B) We fail to reject H₀ at a 2% level of significance, since 104 is contained within the 98% confidence interval.
 - (C) We reject H₀ at the 1% level of significance, since 100 is not contained within the 98% confidence interval.
 - (D) We fail to reject H₀ at the 4% level of significance, since 104 is contained within the 98% confidence interval.
 - (E) We reject H_0 at a 2% level of significance, since 100 is not contained within the 98% confidence interval.

- 5. A statistician conducted a test of $H_0: \mu = 1$ vs. $H_a: \mu > 1$ for the mean μ of some population. Based on the gathered data, the statistician concluded that H_0 could be rejected at the 1% level of significance. Using the same data, which of the following statements must be **true**?
 - (I) A test of $H_0: \mu = 1$ vs. $H_a: \mu > 1$ at the 10% level of significance would also lead to rejecting H_0 .
 - (II) A test of $H_0: \mu = 0$ vs. $H_a: \mu > 0$ at the 1% level of significance would also lead to rejecting H_0 .
 - (III) A test of $H_0: \mu = 1$ vs. $H_a: \mu \neq 1$ at the 1% level of significance would also lead to rejecting H_0 .
 - (A) I only
 - (B) I and II only
 - (C) I and III only
 - (D) II and III only
 - (E) I, II and III

6. We conduct a hypothesis test of $H_0: \mu = 20$ vs. $H_a: \mu \neq 20$ for the mean of some population at the 5% level of significance. Using a sample of size 30, we determine that H_0 should be rejected if $\bar{x} < 17$ or $\bar{x} > 23$. The power of the test against the alternative $H_a: \mu = 25$ is calculated to be 0.8621.

Which of the following statements is true?

- (A) If we had instead used a sample size of 50, the probability of a Type II error would increase.
- (B) If we used a 5% level of significance and a sample of size 50, the power of the test would decrease.
- (C) The power of the test against the alternative $H_a: \mu = 15$ is 0.1379.
- (D) If we had instead used a 1% level of significance, the probability of a Type II error would decrease.
- (E) If we had instead used a 10% level of significance, the power of the test would increase.

7. The Winnipeg Transit Commission claims that the average time taken by the Number 60 bus to travel from the University of Manitoba to downtown is 27 minutes. A student who takes this route often believes that the true mean time is greater than 27 minutes. The student records the time for a sample of five trips. These trips had a mean time of 30 minutes and a standard deviation of 4 minutes. Suppose it is known that trip times have a normal distribution.

The P-value for the appropriate test of significance to test the student's suspicion is:

- (A) between 0.01 and 0.02.
- (B) between 0.02 and 0.025.
- (C) between 0.025 and 0.05.
- (D) between 0.05 and 0.10.
- (E) between 0.10 and 0.15.

8. Bottles of a certain brand of apple juice are supposed to contain 300 ml of juice. There is some variation from bottle to bottle because of imprecisions in the filling machinery. A consumer advocate inspector selects a random sample of 36 bottles and tests the hypotheses $H_0: \mu = 300$ vs. $H_a: \mu < 300$ at the 10% level of significance. Fill volumes are known to follow a normal distribution with standard deviation 3 ml. What is the power of the test if the true mean fill volume is actually 298 ml?

(A) 0.9925

(B) 0.9943

(C) 0.9957

(D) 0.9967

Sample Midterm Test - B

9. In a study of iron deficiency among infants, random samples of infants following different feeding programs were compared. One group contained breast-fed infants, while the children in another group were fed a standard baby formula without any iron supplements. Summary results on blood hemoglobin levels at 12 months of age are shown below.

Group	Sample Size	Sample Mean	Sample Std. Dev.
Breast-fed	7	10.1	1.3
Formula-fed	11	9.4	1.8

A 98% confidence interval for the difference in true mean hemoglobin levels for the two populations of infants is:

(A)
$$0.7 \pm 2.00$$

(B)
$$0.7 \pm 2.04$$

(C)
$$0.7 \pm 2.08$$

(D)
$$0.7 \pm 2.12$$

(E)
$$0.7 \pm 2.15$$

The next two questions (10 and 11) refer to the following:

Eight males and eight females volunteered to be part of an experiment. All 16 people were Caucasian and between the ages of 18 and 24. Each of the eight male participants was randomly assigned a night club, and each of the eight females was randomly assigned to one of these same eight night clubs. One Friday night, all 16 people went out to the bar. Each person then went up to the bar to order a drink (within 5 minutes of one another, with the order randomly determined.) The time (in seconds) until each customer was served was recorded. The table below contains some information that may be helpful:

FemalesMalesDifference
$$(d = \text{Female} - \text{Male})$$
mean = 48mean = 62mean = -14std. dev. = 18std. dev. = 23std. dev. = 15

The question of interest in this experiment is whether females receive faster service at bars on average than males. Assume the appropriate normality assumptions are satisfied.

- 10. What are the hypotheses for the appropriate test of significance?
 - (A) $H_0: \mu_d = 0$ vs. $H_a: \mu_d < 0$
 - (B) $H_0: \bar{X}_d = 0$ vs. $H_a: \bar{X}_d > 0$
 - (C) $H_0: \mu_F = \mu_M \text{ vs. } H_a: \mu_F > \mu_M$
 - (D) $H_0: \bar{X}_d = 0$ vs. $H_a: \bar{X}_d < 0$
 - (E) $H_0: \mu_d = 0$ vs. $H_a: \mu_d > 0$

- 11. What is the P-value for the appropriate test of significance?
 - (A) between 0.005 and 0.01
 - (B) between 0.01 and 0.02
 - (C) between 0.02 and 0.025
 - (D) between 0.025 and 0.05
 - (E) between 0.05 and 0.10

The next two questions (12 and 13) refer to the following:

The following data represent the fat content found in samples of two popular brands of ice cream:

Brand			Fat			sample mean	sample variance
A	6.3	5.1	6.8	6.9	7.4	6.50	0.77
В	6.3	5.7	5.9	6.4	5.1	5.88	0.27

- 12. We would like to conduct a hypothesis test to determine whether the true mean fat content differs for the two brands of ice cream. Assuming fat content follows a normal distribution for both brands, we should use:
 - (A) a matched pairs t test with 4 degrees of freedom.
 - (B) a pooled two-sample t test with 8 degrees of freedom.
 - (C) a conservative two-sample t test with 7 degrees of freedom.
 - (D) a pooled two-sample t test with 9 degrees of freedom.
 - (E) a conservative two-sample t test with 8 degrees of freedom.

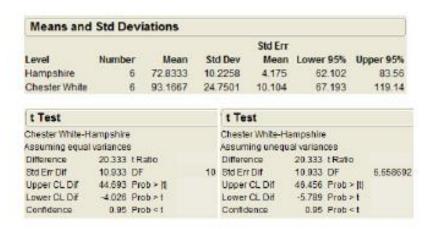
Sample Midterm Test - B

- 13. The P-value for the appropriate test of significance is calculated to be 0.21. We interpret this value to mean:
 - (A) If the true mean fat content was equal for the two brands, the probability of incorrectly concluding that the means differ would be 0.21.
 - (B) The probability that the true mean fat content is equal for the two brands is 0.21.
 - (C) The probability that the true mean fat content differs for the two brands is 0.21.
 - (D) If the true mean fat content were equal for the two brands, the probability of observing a difference in sample means at least as extreme as 0.62 would be 0.21.
 - (E) If the true mean fat content differed for the two brands, the probability of observing a difference in sample means at least as extreme as 0.62 would be 0.21.

14. The following table displays the serum calcium measurements for samples of two breeds of cows. Serum calcium levels are known to follow a normal distribution for both breeds.

> Chester White 116 112 82 63 117 69 Hampshire 62 79 80 85 60 71

We would like to conduct a hypothesis test to determine whether the true mean serum calcium level differs for the two breeds. Some JMP output that may be helpful is shown below:



The P-value for the appropriate test of significance is:

- (A) between 0.01 and 0.02
- (B) between 0.025 and 0.05
- (C) between 0.05 and 0.10
- (D) between 0.10 and 0.20
- (E) between 0.20 and 0.30

15. A student would like to conduct a hypothesis test to determine whether the true mean exam score for students in Dr. E. Zee's class is greater than that for student's in Dr. D. Ficult's class. Exam scores are known to follow a normal distribution for each of the two classes. The student selects random samples of students from each professor's class. Some summary statistics for their exam scores are shown below:

Group	Sample Size	Sample Mean	Sample Std. Dev.
Dr. E. Zee	14	74	6
Dr. D. Ficult	10	53	14

What is the value of the test statistic for the appropriate test of significance?

- (A) 3.77
- (B) 4.46
- (C) 5.04
- (D) 6.62
- (E) 7.13

- 16. In which of the following situations are the matched pairs t procedures appropriate?
 - (I) We would like to compare the mean number of mosquitoes caught in two different types of mosquito traps. A sample of 20 locations is selected in Winnipeg, and one of each type of trap is placed at each location.
 - (II) We would like to compare the mean commuting times from home to work for workers in Winnipeg and Toronto. A sample of 30 workers in each city is selected.
 - (III) We would like to compare the mean summer temperatures in Winnipeg and Brandon (Manitoba's second largest city, 200 km west of Winnipeg). On a sample of 25 days, we measure the temperature in each city.
 - (A) I only
 - (B) II only
 - (C) III only
 - (D) I and II only
 - (E) I and III only

17. A horticulturist is investigating the phosphorous content of tree leaves from three different varieties of apple trees. Phosphorous content is known to follow a normal distribution for each of the three varieties. Random samples of four leaves from each of the three varieties are analyzed for phosphorous content. Population variances are known to be equal for all three varieties. We would like to test the hypothesis of equal population means for the three varieties at the 10% level of significance. The critical value for the appropriate hypothesis test is:

(A) 1.36

(B) 2.81

(C) 3.01

(D) 5.22

(E) 9.38

- 18. Which of the following statements about the analysis of variance F test is false?
 - (A) The test statistic compares the variability between sample means to the variability within individual samples.
 - (B) The test is "many-sided", as there are many different inequalities in means that will lead us to reject the null hypothesis.
 - (C) The test gives the same results we would observe if we compared each pair of means separately using pooled two-sample t tests.
 - (D) The ANOVA procedures are quite robust against non-normality.
 - (E) The ANOVA procedures are not very sensitive to the case of unequal population variances.

- 19. We take simple random samples from two normally distributed populations and measure the value of some variable X. We conduct a pooled two-sample t test to determine whether there is evidence that the population means differ. We calculate a test statistic of t=2.47 and a P-value of 0.04. Suppose we had instead conducted the test using an analysis of variance. What would be the value of the test statistic and the P-value?
 - (A) 6.10 and 0.04
 - (B) 2.47 and 0.0016
 - (C) 1.57 and 0.04
 - (D) 6.10 and 0.0016
 - (E) 2.47 and 0.20

- 20. We are conducting an analysis of variance to compare the means of four populations. In conducting this test, we will commit a Type I error if we:
 - (A) fail to conclude that all four means differ when in fact this is the case.
 - (B) conclude that at least one of the means differs when in fact they are all equal.
 - (C) conclude that all four means differ when in fact they are all equal.
 - (D) fail to conclude that at least one mean differs when in fact this is the case.
 - (E) conclude that one mean differs when in fact all four means differ.

The next three questions (21 to 23) refer to the following:

A medical researcher wants to compare three different techniques designed to lower blood pressure in patients with hypertension. Five subjects are assigned to each of the three groups. The first group exercises, the second group meditates and the thrid group takes medication. After five weeks, the reduction in each person's blood pressure is recorded. The researcher wants to determine if there is any difference in the effectiveness of the three techniques. The ANOVA table (with some values missing) is shown below:

Source of Variation	df	Sum of Squares	Mean Squares	F
Groups		102		
Error				
Total		282		

21. What is the P-value of the test?

- (A) less than 0.001
- (B) between 0.001 and 0.01
- (C) between 0.01 and 0.025
- (D) between 0.025 and 0.05
- (E) between 0.05 and 0.10

99	What is	the estimate	e of the common	variance	for the three	treatmente
44.	wnat is	tne estimate	e of the common	variance	for the three	treatments:

(A) 4

(B) 7

(C) 13

(D) 15

(E) 51

23. We would like to construct a 95% confidence interval for the difference in the mean response for the exercise and medication groups. The margin of error for the appropriate confidence interval is:

(A) 5.25

(B) 5.34

(C) 5.65

(D) 9.53

(E) 12.49

Sample Midterm Test - B

The next three questions (24 to 26) refer to the following:

A coffee store owner compiles the following information:

- A customer gets a coffee (C) in 35% of the store's transactions.
- A customer gets a donut (D) in 40% of the store's transactions.
- In 45% of the store's transactions, a customer gets a coffee or a muffin (M).
- In 61% of the store's transactions, a customer gets a donut or a coffee.
- In 10% of the store's transactions, a customer gets a donut and a muffin.
- In 26% of the store's transactions, a customer gets a coffee and a muffin.
- In 4% of the store's transactions, a customer gets a donut, a coffee and a muffin.

24. What is the probability that a randomly selected customer gets a muffin?

(A) 0.29

(B) 0.36

(C) 0.41

(D) 0.44

25.	What is	the	probability	that	a	$\operatorname{customer}$	who	buys	a	${\it coffee}$	also	buys	a	${\rm donut}$	and	a
	muffin?															

(A) 0.04

(B) 0.08

(C) 0.11

(D) 0.14

- 26. Which of the following statements is **true**?
 - (A) The events C and D are independent.
 - (B) The events C and D are mutually exclusive.
 - (C) The events C and M are independent.
 - (D) The events C and M are mutually exclusive.
 - (E) The events D and M are independent.

- 27. A tourist is flying home from Cairo, Egypt to Winnipeg. She must change planes in Berlin, London and Toronto. Her suitcase is placed on her plane flying from Cairo to Berlin. Suppose we have the following facts:
 - 5% of all suitcases are lost at the airport in Berlin.
 - $\bullet~8\%$ of all suit cases are lost at the airport in London.
 - 7% of all suitcases are lost at the airport in Toronto.

What is the probability that the tourist's suitcase arrives safely in Winnipeg?

(A) 0.80

(B) 0.81

(C) 0.82

(D) 0.83

The next two questions (28 and 29) refer to the following:

The following six games are being played in the National Hockey League one night. The values in parentheses are the probabilities of each team winning their respective game:

Game 1: Tampa Bay Lightning (0.47) New York Rangers (0.53) VS. Game 2: Carolina Hurricanes (0.58) New York Islanders (0.42) VS. Game 3: Winnipeg Jets (0.27) Washington Capitals (0.73) VS. Game 4: Chicago Blackhawks (0.60) Dallas Stars (0.40) VS. Game 5: Colorado Avalanche (0.31) Detroit Red Wings (0.69) VS.

Game 6: San Jose Sharks (0.46) vs. Vancouver Canucks (0.54)

28. The outcome of interest is the set of winners for each of the six games. How many outcomes are contained in the sample space?

(A) 12 (B) 32 (C) 36 (D) 64 (E) 128

29. What is the probability that Winnipeg wins or that both New York teams win?

(A) 0.4325

(B) 0.4522

(C) 0.4724

(D) 0.4926

30. The time it takes a student to drive to university in the morning follows a normal distribution with mean 28 minutes and standard deviation 4 minutes. The time it takes the student to drive home from university in the afternoon follows a normal distribution with mean 25 minutes and standard deviation 3 minutes. Morning and afternoon commuting times are known to be independent. What is the probability that the student's total travel time to and from school one day exceeds one hour?

(A) 0.0040

(B) 0.0808

(C) 0.1587

(D) 0.2296

31. It is known that 17% of individuals in some population have blue eyes. If we take a random sample of 12 individuals from this population, what is the probability that four of them have blue eyes?

(A) 0.053

(B) 0.063

(C) 0.073

(D) 0.083

The next two questions (32 and 33) refer to the following:

A small deck of cards contains five red cards, four blue cards and one green card. We will shuffle the deck and select three cards without replacement. Let X be the number of blue cards that are selected. The probability distribution of X is shown below:

$$\begin{array}{c|ccccc} x & 0 & 1 & 2 & 3 \\ \hline P(X=x) & 0.167 & 0.500 & 0.300 & 0.033 \\ \end{array}$$

- 32. What is the variance of X?
 - (A) 0.56
- (B) 0.61
- (C) 0.68
- (D) 0.72
- (E) 0.85

33.	What	would	be	the	variance	of	X	if	we	had	instead	selected	the	three	cards	with
	replacement?															

(A) 0.56

(B) 0.61

(C) 0.68

(D) 0.72

34. The number of goals scored in a hockey game follows a Poisson distribution with a mean of 0.1 per minute. What is the probability that at least two goals are scored in a 60-minute game?

(A) 0.9554

(B) 0.9723

(C) 0.9826

(D) 0.9899

35. A random variable X follows a Poisson distribution with parameter λ . If we know that P(X=1)=P(X=3), then what is the value of λ ?

(A) $\sqrt{2}$

(B) $\sqrt{3}$

(C) $\sqrt{5}$

(D) $\sqrt{6}$

(E) $\sqrt{8}$